VERIFICATION OF THE NEUTRON MIRROR CAPABILITIES IN MCNPX VIA GOLD FOIL MEASUREMENTS AT THE EIGER INSTRUMENT BEAMLINE AT THE SWISS SPALLATION NEUTRON SOURCE (SINQ)

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Abstract
The EIGER triple-axis thermal neutron spectrometer beamline contains “supermirror” neutron guides, which preferentially reflect low-energy neutrons toward the EIGER spectrometer that come from the ambient temperature, light water neutron source in SINQ. Gold foil measurements have been performed at the EIGER beamline in 2013. This process can be modeled from incident proton to thermal neutron exiting the EIGER beamline by using the neutron mirror capabilities of MCNPX, which should be more accurate than simulations with simplified neutron source distributions and geometry representations. The supermirror reflectivity parameters have been measured previously and are used in MCNPX 2.7.0 to reproduce the activity measured from the gold foil irradiation, verifying the neutron mirror modeling capabilities in MCNPX 2.7.0.

INTRODUCTION
EIGER is a triple-axis thermal neutron spectrometer that looks at the light water scatterer inside SINQ, a spallation neutron source driven by a continuous 590 MeV proton beam at the Paul Scherrer Institut in Villigen, Switzerland. The incoming protons impinge on a lead target cooled with heavy water, producing high energy neutrons. These neutrons are moderated by the tank of D₂O surrounding the target. The “water scatterer” is a set of seven vertical aluminum tubes 25 cm away from the center of the target that contain ambient temperature light water. These tubes act as a scattering medium to send thermal neutrons streaming through low pressure nozzles towards neutron instruments.

The neutron guide that delivers thermal neutrons from the water scatterer towards the EIGER instrument is internally covered with neutron “supermirrors”. These mirrors are reflective to low-energy neutrons, and allow the guide to transport neutrons with small divergence instead of only neutrons with trajectories parallel to the guide axis, increasing neutron extraction efficiency. The reflectivity of the mirrors are described by Eq. 1 where \( R_0 \) is nominal reflectivity, \( Q_c \) is the critical momentum transfer, \( m \) is the angular extension parameter, \( \alpha \) is reflectivity declination parameter, and \( W \) is the reflectivity edge width [1].

\[
R(Q) = \begin{cases} 
\frac{R_0}{1 - \tanh \left( \frac{Q - m Q_c}{W} \right)} & \text{if } Q > Q_c \\
\frac{1 - \tanh \left( \frac{Q - m Q_c}{W} \right)}{1 - \alpha (Q - Q_c)} & \text{if } Q \leq Q_c 
\end{cases}
\]

This reflectivity model is used by McStas and has been previously implemented in patched version of MCNPX 2.5.0 [1]. The patch has recently been ported to MCNPX 2.7.0 [4] and debugged for MPI parallelism. The parallelized reflectivity capabilities now allow the neutron flux gains to be completely modeled in MCNPX 2.7.0. This capability is demonstrated by comparing the calculated activation of an array of gold foils exposed to the EIGER beam to experimental results.

GOLD FOIL MEASUREMENT
The vertical array of six gold foils shown in Figure 1 were exposed to the EIGER beam in December, 2013.

Figure 1: Gold foil array used in the measurements.

The foils were placed near the monochromator position at EIGER. The foils are 25 mm in diameter and 30 mm center-to-center. The blue marker lines in the figure show the approximate extent of the neutron guide. The average current on the SINQ target during the irradiation was 200\( \mu \)A, and the foils were exposed for 5 minutes. After irradiation, activation analysis was performed using a gamma spectrometer.

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**EIGER BEAMLINE SIMULATION**

The MCNPX model geometry is shown in Figure 2. The major components are the lead target, the moderator tank, the water scatterer, the in-tank nozzles, the sapphire crystal, the neutron guide, and the shielding around SINQ and EIGER. The MCNPX simulation used the relevant $S(\alpha, \beta)$ data, including those for the crystal sapphire [5]. The MCNPX model for the water scatterer was created from CAD models using the MCAM interface code developed by the FDS Team, China [6].

![Figure 2: MCNPX geometry of the EIGER beamline with important elements highlighted.](image)

The total fraction of neutrons that make it to EIGER is small ($\sim 10^{-6}$ per proton), and the low absorption means neutrons undergo many thousands of interactions before they are lost, on average. This required the use of multiple variance reduction techniques in MCNPX. The first technique used was mesh-based neutron weight windows. A spherical mesh centered around the water scatterer with fine divisions at small radii and in the direction of the target was used. The values of the mesh were optimized based on the response of a point detector tally at the measurement position. Point detectors are not able to capture the reflectivity effects since they estimate non-interaction along a straight line. Therefore, neutrons were propagated down the guide using a DXTRAN sphere. At every collision, the sphere forces a fraction of a neutron’s weight to be placed at the sphere radius. The weight is proportional to the probability of the neutron scattering in the direction of the sphere and arriving there without colliding again. After placement, these “uncollided” neutrons are transported normally [4]. The DXTRAN sphere was placed around the sapphire crystal and a surface source was written from the downstream surface of the crystal. The calculated spatial distributions of the thermal neutron current within a 5° cone normal to the water scatterer and the sapphire crystal are shown in Figure 3. The SINQ target is on the left side in both figures. The neutron current spectra at the water scatterer and after the sapphire crystal are shown in Figure 4. The post-sapphire distribution was used as the source term in a set of subsequent calculations with the neutron guide reflectivity turned on and off. The surface source was sampled repeatedly with different initial random number seeds in order to capture the full weight variance of the sapphire surface source at the measurement point. Much effort was made to keep the simulations as high-fidelity as possible; no spectral or spatial approximations were made with regard to the neutron population, and no geometrical simplifications were knowingly made.

![Figure 3: The thermal neutron current distribution in a 5° cone normal to the EIGER-facing surface water scatterer (left) and the downstream surface of the sapphire crystal (right). The solid magenta curve shows the approximate view of the EIGER nozzle and the solid black rectangle shows the approximate view of the sapphire crystal.](image)

**ACTIVATION RESULTS**

The neutron energy spectrum at the measurement point was calculated with 256 equi-log bins from $10^{-12}$ to 600 MeV for cases with the guide reflectivity turned on and off.
The spectra and reflectivity gain factors (ratio of the spectra) from these two sets of calculations are shown in Figure 5.

Figure 5: The average flux spectra at the gold foil irradiation position with the guide reflectivity turned on and off in MCNPX (top), and the energy dependence of the reflectivity gain (bottom).

The reflectivity gain goes above unity below 200 meV and increases to 2.5 at 3 meV. Below 3 meV, the statistics of the simulation start to become unreliable. The gold \((n,\gamma)\) macroscopic cross section was then averaged to the same binning as the spectra, multiplied by the spectra, and summed to determine the total reaction rate in the gold foils per incident proton on the SINQ target. The experimental irradiation and analysis parameters were then used to calculate the specific activity in the foils. The results are shown in Figure 6.

Figure 6: The measured and calculated activity of the gold foils (top), and the relative difference in gain between the measured and ideal cases (bottom).

It can be seen that the two calculated activity curves (ideal and no reflectivity) bracket the measured values, and that the highest gain factor is at the vertical center of the guide opening. The lower plot in Figure 6 shows the relative difference of the ideal and measured gain factors. The flux is less than 50% of the ideal value at the vertical center of the guide, and about equal to the non-reflective case at the top and bottom of the guide. The average value is 20% if the -7.5 cm value is not considered. The activity for this foil departs from the trend and may be the result of an incorrect measurement of its mass.

CONCLUSION

The calculated results confirm that reflective neutron guides can now be completely modeled in MCNPX 2.7.0, and indicate that the EIGER supermirrors are operating at 20% of “ideal” capacity.

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REFERENCES


